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Q1] Select the correct answer (45 points, 3 points each):

1) What is the number represented of the binary words 10010010, assuming the representation is in Two's complement

- A. -110
- B. 110
- C. -109
- D. -108
- E. None

$$\begin{array}{r}
 \text{10010010} \\
 \text{+ 01101101} \\
 \hline
 \text{11111111} \\
 \text{+ 00000001} \\
 \hline
 \text{11111110} \\
 \hline
 \text{64} \\
 \text{32} \\
 \hline
 \text{96}
 \end{array}$$

2) The number (161)₁₀ is equivalent to:

- A. (11)₁₆
- B. (1A)₁₆
- C. (A1)₁₆
- D. (AA)₁₆
- E. None

$$\begin{array}{l}
 1 \times 16^0 + 1 \times 16^1 \\
 1 \times 16 + 1 \\
 16 + 1 = 17 \\
 17 \times 16 = 272 \\
 272 + 1 = 273
 \end{array}$$

3) The number (55)₈ is equivalent to:

- A. (2D)₁₆
- B. (D2)₁₆
- C. (B1)₁₆
- D. (1B)₁₆
- E. None

$$\begin{array}{r}
 4218 \times 2^1 \\
 101101 \\
 \hline
 2 \quad 13 \\
 230
 \end{array}$$

4) Using BCD code, when a computer adds (01001001)₂ + (10000000)₂ the result of this addition:

- A. is a correct BCD number.
- B. must be corrected by adding (00000110)₂.
- C. must be corrected by adding (01100000)₂.
- D. must be corrected by adding (01100110)₂.
- E. is wrong and can't be corrected.
- F. None

$$\begin{array}{r}
 01001001 + \\
 10098009 \\
 \hline
 11001001 \\
 \hline
 8421 + 8421 \\
 \hline
 01100000
 \end{array}$$

5) Even parity is:

- A. an extra bit added to make the total number of ones even to detect odd number of errors.
- B. an extra bit added to make the total number of ones even to detect even number of errors.

$$\begin{array}{r}
 20 \times \\
 2 \overline{) 160} \\
 \underline{160} \\
 0
 \end{array}$$

- C. an extra bit added to make the total number of ones odd to detect odd number of errors.
- D. an extra bit added to make the total number of ones odd to detect even number of errors.
- E. an extra bit added to make the total number of ones even to detect any number of errors.

6) Given $F(x, y, z) = \prod(0, 3, 4, 7)$, and G is the complement of F , then:

A. $G(x, y, z) = \sum(0, 1, 2, 3, 5, 7)$

B. $G(x, y, z) = \prod(0, 3, 4, 7)$

C. $G(x, y, z) = \sum(1, 2, 5, 6)$

D. $G(x, y, z) = \sum(0, 3, 4, 7)$

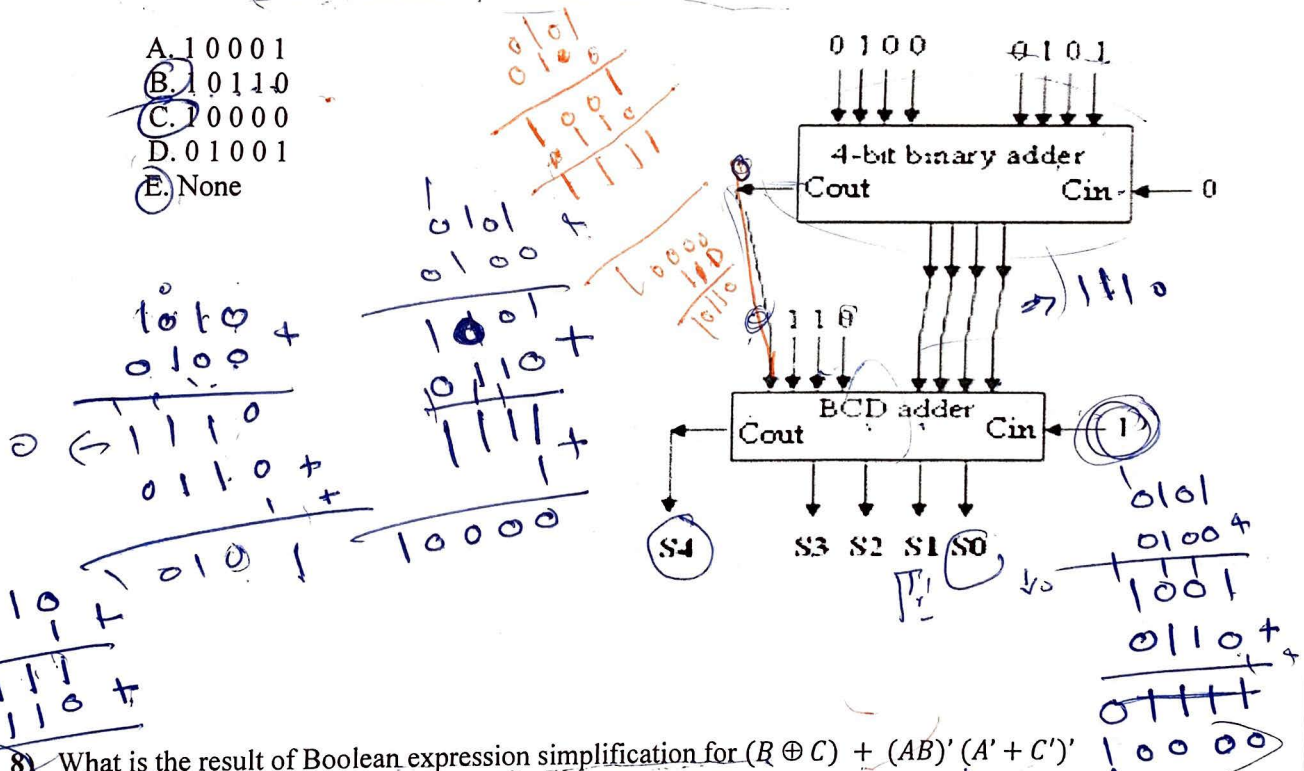
E. None

$\sum(1, 2, 5, 6)$
 $\prod(0, 3, 4, 7)$

$F' = \sum(1, 2, 5, 6)$
 $\prod(0, 3, 4, 7)$

7) The binary value of $S_4 S_3 S_2 S_1 S_0$ in the circuit beside is

- A. 10001
- B. 10110
- C. 10000
- D. 01001
- E. None



8) What is the result of Boolean expression simplification for $(B \oplus C) + (AB)'(A' + C)'$

- A. $B \oplus C$
- B. $A \oplus C$
- C. $(B \oplus C)'$

$B'C + BC' + A' + B' (AC)$

$B'C + BC' + AA'C + ACB'$

$B'C (1 + A) + BC'$

$B'C + BC' + A' + B' \cdot AC$

$B'C + BC' + AA'C + ACB'$

$CB' + BC'$

D. $(A \oplus B)'$

E. None

9) In the shown K-map, the essential prime implicant is

A. AC

B. CD

C. $A'D$

D. $A'C'$

E. None

		CD			
	AB	00	01	11	10
00	1	X	1	X	
01	1	X	1		
10			1	X	
11			X	X	

10) The output Y of the circuit computes

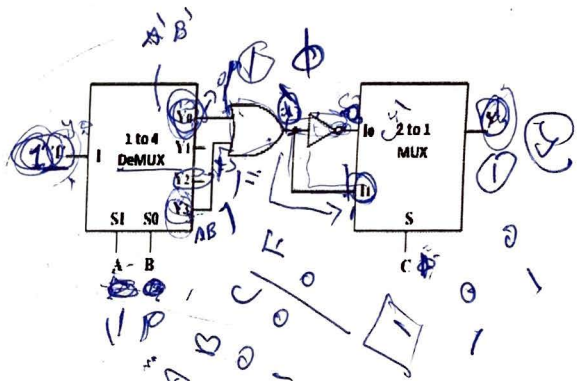
A. the sum bit of a full adder

B. the carry bit of a full adder

C. the complement of A

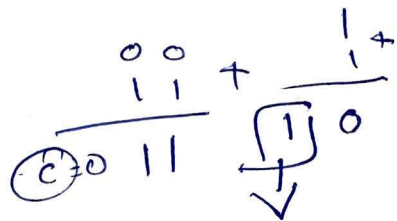
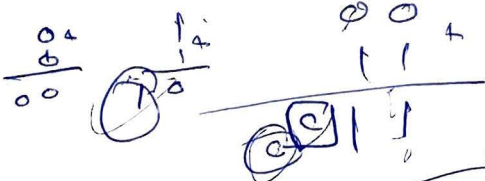
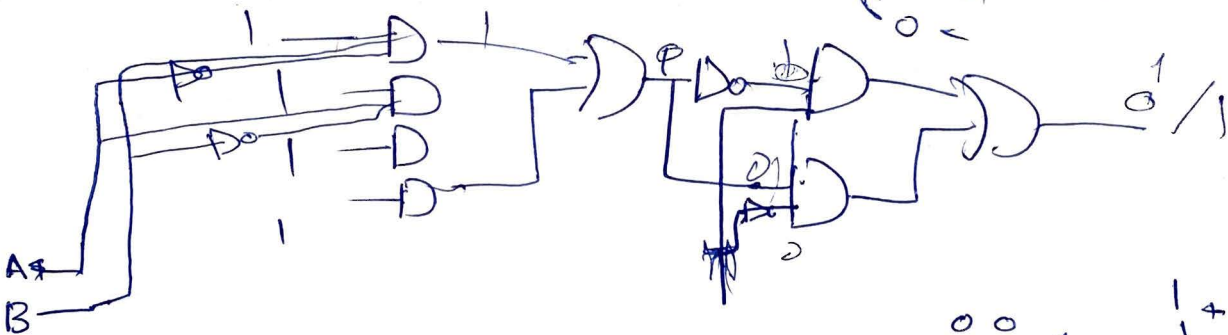
D. Complement of B

E. None



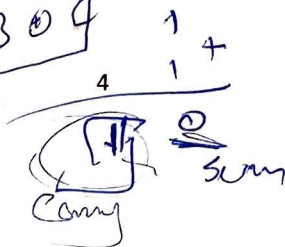
$y_0 \quad y_3$

A B -



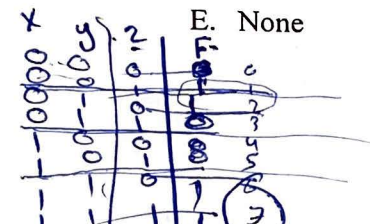
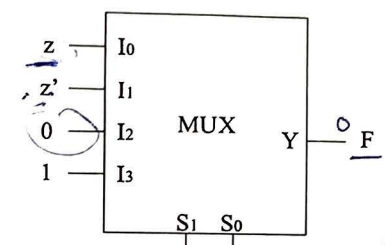
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	1

$A \oplus B \oplus C$



11. Which function F is implemented by using this 4X1 Multiplexer

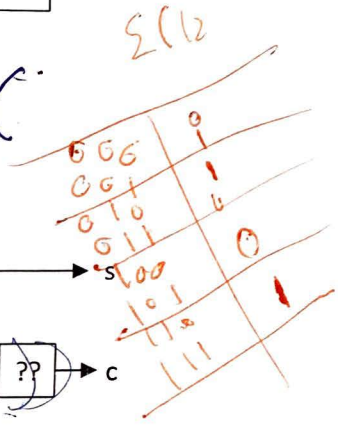
- A. $F(x, y, z) = \sum(0, 3, 4, 5)$
- B. $F(x, y, z) = \sum(1, 3, 6, 7)$
- C. $F(x, y, z) = \sum(1, 2, 6, 7)$
- D. $F(x, y, z) = \sum(1, 2, 5, 7)$
- E. None



1, 2, 6, 7

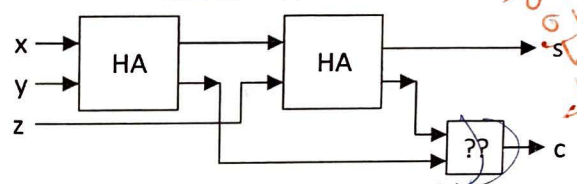
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$\Sigma()$



12. Implementation of full adder with two half adders and an ___ gate

- A. OR
- B. NOR
- C. XOR
- D. XNOR
- E. None

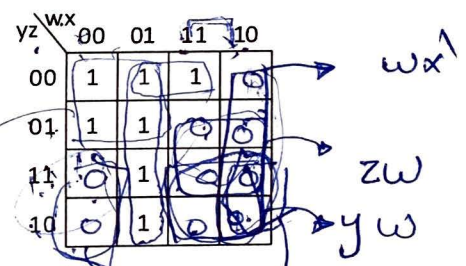


FA =

13. For the function F, the minimum product of sums expression

- A. $F = w'x + w'y' + xy'z'$
- B. $F = x'y + wx' + wz + wy$
- C. $F = (x+y')(w'+x)(w'+z')(w'+y')$
- D. $F = (w+x')(w+y)(x'+y+z)$
- E. None

8x1
4x1



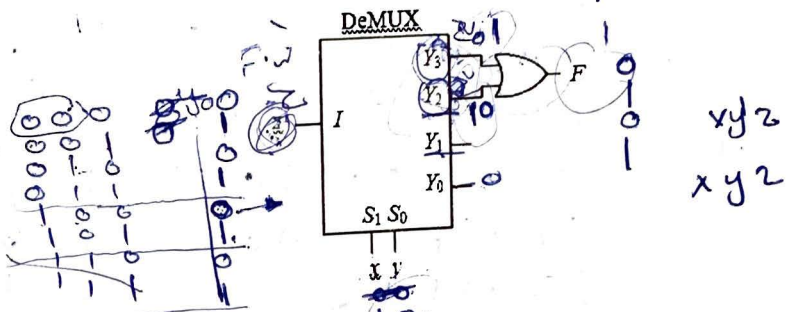
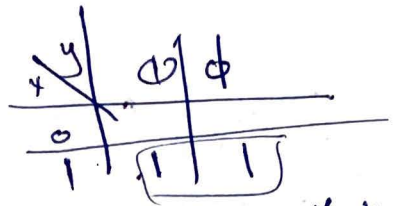
$$= y'w' + w'x + y'z'x$$

$$(w+x') \cdot (z+w) \cdot (y+z) \cdot (y+x')$$

$$(y+w + w+x' + y+z+x')$$

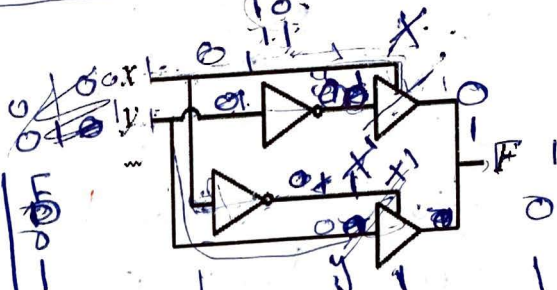
14. For the shown Demux, the Boolean function is

- A. $F = x'y'z + xyz$
- B. $F = x'yz + xyz$
- C. $F = xy'z + xyz$
- D. $F = xy'z' + xyz$
- E. None



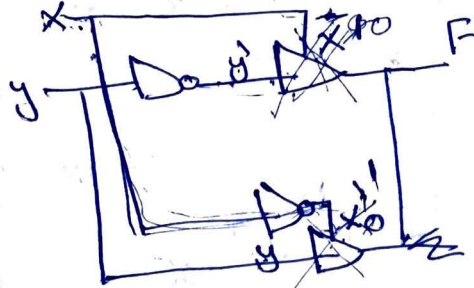
15. For the shown circuit the function F is

- A. $F = X \text{ AND } Y$
- B. $F = X \text{ OR } Y$
- C. $F = X \text{ XOR } Y$
- D. $F = X \text{ XNOR } Y$
- E. None



1	2	3	4	5	6	7	8	9	10
A	C	A	C	B	A	C	A	D	B

11	12	13	14	15
C	A	D	C	B

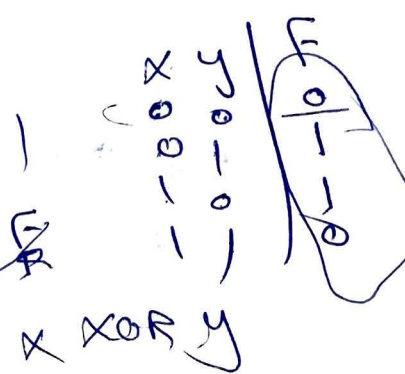


x	y	F
0	0	0
0	1	1
1	0	1
1	1	0

x=1 F=y
x=0 F=y

$xy'z + xyz$

x=1 y=y
x=0 y=y



part essential of

$$F = P_7 + P_6 + P_5 + P_4 + P_3 + P_2 + P_1$$

or P₆ or P₅ or P₄ or P₃ or P₂ or P₁

	P1	P2	P3	P4	P5	P6	P7	P8
P1	1							
P2		1						
P3			1					
P4				1				
P5					1			
P6						1		
P7							1	
P8								1

P1	1	0	0	0	0	0	0
P2	0	1	0	0	0	0	0
P3	0	0	1	0	0	0	0
P4	0	0	0	1	0	0	0
P5	0	0	0	0	1	0	0
P6	0	0	0	0	0	1	0
P7	0	0	0	0	0	0	1
P8	0	0	0	0	0	0	0

P1	1	0	0	0	0	0	0
P2	0	1	0	0	0	0	0
P3	0	0	1	0	0	0	0
P4	0	0	0	1	0	0	0
P5	0	0	0	0	1	0	0
P6	0	0	0	0	0	1	0
P7	0	0	0	0	0	0	1
P8	0	0	0	0	0	0	0

3

2

Q2] 18 points

Simplify using QM Tabulation method the following function

$$F(A,B,C,D) = \sum m(0,1,2,3,5,7,8,10,14,15)$$

- 0 = 0000 ✓
- 1 = 0001 ✓
- 2 = 0010 ✓
- 3 = 0011 ✓
- 5 = 0101 ✓
- 7 = 0111 ✓
- 8 = 1000 ✓
- 10 = 1010 ✓
- 14 = 1110
- 15 = 1111

①

✓ 0	0000	✓ (0,1)	000-	(0,2,1,3)	00--
✓ 1	0001	✓ (0,2)	00-0	(0,2,2,3)	00--
✓ 2	0010	✓ (0,8)	-000	(0,2,8,16)	-0-0
✓ 3	0011	✓ (1,3)	00-1	(0,8,2,10)	-0-0
✓ 5	0101	✓ (1,5)	0-01	(1,3,5,7)	0--1
✓ 10	1010	✓ (2,3)	00-1	(2,3,5,7)	0--1
✓ 7	0111	✓ (2,16)	10-0		
✓ 14	1110	✓ (3,10)	0-11		
15	1111	✓ (3,7)	01-1		
		✓ (5,7)	1010		
		✓ (10,14)	1111		
		✓ (7,15)	111-		
		✓ (14,15)			

- ~~PI1 = 000- (0,1)~~
- ~~PI2 = 0-01 (1,5)~~
- ~~PI3 = 01-1 (5,7)~~
- ~~PI4 = 1-10 (10,14)~~
- ~~PI5 = 111- (7,15)~~
- ~~PI6 = 111- (14,15)~~

← البقى

Q4] 10 points

Many offices and buildings use combination locks to control entry. As the design engineer of the *Wonderful Door Security Company*, you are asked to implement a door security system by using a card reader. There are four inputs to the card reader: inputs X, Y, and Z are used to validate the correct door code and input V is used to check if the card reader is still valid. After the card reader is being read by the system, there are three outputs to this system: alarm (A), door open (D), and Error (E). Door (D) will only open when the decimal value of the binary inputs (X, Y, Z) is odd (عدد گزدي) AND the card reader is valid. The Error (E) signal goes on when the code on the card is correct (i.e. decimal value equal to odd) but the card is no longer valid. Finally, the alarm (A) will trigger when the code is incorrect (i.e. decimal value equal to even). Derive the truth table only

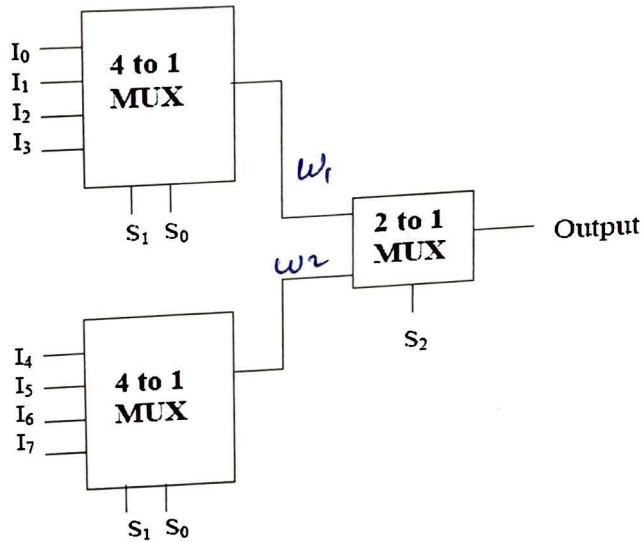
valid $V=1$
invalid $V=0$

	X	Y	Z	V	A	D	E
0	0	0	0	0	1	0	0
1	0	0	0	1	0	0	0
2	0	0	1	0	0	0	0
3	0	0	1	1	0	1	0
4	0	1	0	0	0	0	0
5	0	1	0	1	0	0	0
6	0	1	1	0	0	0	0
7	0	1	1	1	0	1	0
8	1	0	0	0	0	0	0
9	1	0	0	1	0	0	0
10	1	0	1	0	0	0	0
11	1	0	1	1	0	1	0
12	1	1	0	0	0	0	0
13	1	1	0	1	0	0	0
14	1	1	1	0	0	0	0
15	1	1	1	1	0	0	0

$D \Rightarrow$ odd and valid $V=1$
 $A \Rightarrow$ even
 $E \Rightarrow$ odd and invalid $V=0$

Q5] 15 points

For the system shown in the following figure



1. (5 points) Write a Verilog HDL code to describe the module mux4x1
2. (4 points) Write a Verilog HDL code to describe the module mux2x1
3. (6 points) Write a Verilog HDL code to describe the whole system structurally from its subsystems

```

① module mux4x1 ( I0, I1, I2, I3, S0 S0, S1, w1 )
    input I0, I1, I2, I3;
    output w1;
    reg w1;
    always @ ( I0 or I1 or I2 or I3 )
        if ( S1 == 0 && S0 == 0 )
            w1 = I0;
        else
            if ( S1 == 0 && S0 == 1 )
                w1 = I1;
            else
                if ( S1 == 1 && S0 == 0 )
                    w1 = I2;
            else
                if ( S1 == 1 && S0 == 1 )
                    w1 = I3;
endmodule
    
```

14

OK

②

module mux2x1 (w1, w2, s2, output)

input w1, w2, s2;

output output;

reg output;

always @ (w1 or w2 or s2)

if (s2 == 0)

output = w1;

else

if (s2 == 1)

output = w2;

end module;

OK

③

module System (I, S, w1, w2, output)

input [7:0] I;

input [2:0] S;

output w1, w2;

output output;

mux4x1 M (I[0], I[1], I[2], I[3], S[0], S[1], w1);

mux4x1 M2 (I[4], I[5], I[6], I[7], S[0], S[1], w2);

mux2x1 M3 (w1, w2, S[2], output);

end module

OK